A Cousin's Grandson is not Mahram

Q: Hajj-19: Hajj has become Fardh for a grandmother. Can she go for Hajj in the company of her cousin's grandson? She is approximately 50 to 60 years of age

Answer: If a woman has no husband or Mahram to accompany her for Hajj, it will not be Fardh for her to perform the Hajj even though it has become Fardh for her (because she has the means). This means that if she is unable to get a Mahram to accompany her before she passes away, she will not be sinful, but will have to make a bequest stating that Hajj Badal be performed on her behalf.

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